Averages and Means in Elementary Calculus

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Abstract

Recurring student errors that surprisingly yield correct answers provide an opportunity for all to learn. This article highlights a few explorations dealing with averages and means, starting with an example from calculus. From the various confusions over averages in particular, one can glean insight into when and why certain functions behave as they do.

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